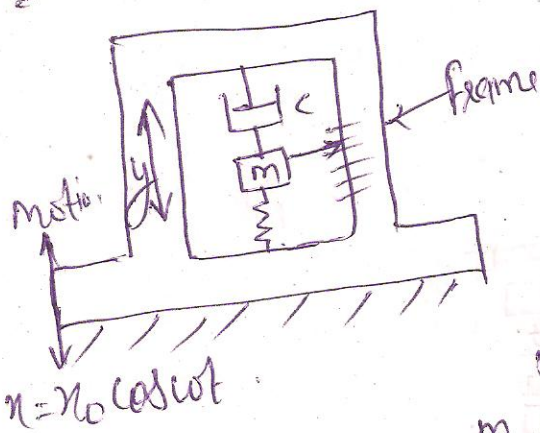


As θ is very small
 \therefore fringe spacing $\Rightarrow p$.

* Absolute motion or vibration devices :-



In these devices the base of the device or transducer is attached to the object whose motion or vibrations are to be measured. Inside transducer a mass m is supported on spring with damper of coefficient c . The motion of mass relative to the mass of object base will give indication of motion of object & in turn output also.

Let $n = n_0 \cos \omega t$
 where $n_0 =$ Amplitude of motion, $\omega =$ circular frequency ($= 2\pi f$)
 $t =$ time variable

\therefore Equation of motion of mass

$$m\ddot{y} = -c(\dot{y} - \dot{n}) - k(y - n)$$

$y - n = z =$ mass relative to frame

The equation may be written as

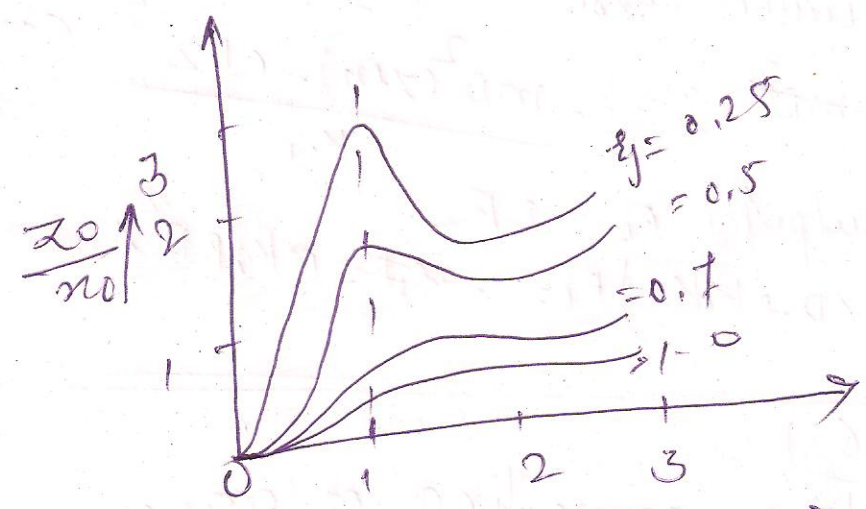
$$m\ddot{z} + c\dot{z} + kz = m\omega^2 n_0 \cos \omega t$$

For steady state value
 $z = z_0 \cos(\omega t - \phi)$

$$\text{Amplitude } z_0 = \frac{m\omega^2 n_0}{\sqrt{(k - m\omega^2)^2 + (c\omega)^2}}$$

$$\text{Amplitude Ratio } \frac{z_0}{n_0} = \frac{r^2}{\sqrt{(1 - r^2)^2 + (2\zeta r)^2}}$$

$\gamma = \frac{c}{2\omega_n m}$ $\sqrt{\frac{k}{m}} = \text{Undamped natural freq. } \omega_n$ (3)
 $\omega_n = \text{critical freq.}$
 $\xi = \frac{c}{2\sqrt{k m}} = \text{damping ratio}$



It can be seen that at $r = \omega/\omega_n \rightarrow \xi = 0.7$ the curves are flat & $r > \sqrt{2}$

The eqn can also be written as

$$\frac{\omega_n^2 z_0}{\omega^2 n_0} = \frac{\delta}{\sqrt{(k - r^2 m)^2 + (2\xi r)^2}}$$

or $\frac{\omega_n^2 z_0}{A_0} = n$

Where $A_0 = \omega_n^2 n_0 = \text{amplitude acceleration of object.}$

* Force balance type seismic devices :-

Unlike in the seismic devices mechanical spring is not used. An electromagnetic actuator and force is applied to mass m . At equilibrium output current i & voltage E produce across R being the output & measure of input motion x .